# **18 Electric fields**

## 18.1 Electric fields and field lines

#### Candidates should be able to:

- understand that an electric field is an example of a field of force and define electric field as force per unit positive charge
- 2 recall and use F = qE for the force on a charge in an electric field
- 3 represent an electric field by means of field lines
  - Electric field strength is defined as the electrostatic force per unit positive charge acting on a stationary point charge at that point.
  - You can find the electric field strength (E) with the following equation

$$E = \frac{F}{q}$$

Here F is the electrostatic force on the charge (N) and q is the charge (C).

• Electric field is a vector quantity with SI unit of NC<sup>-1</sup>



- Opposite charges attract each other.
- Like charges repel each other.
- The electric field equation can be rearranged for the force (F) on a charge (q) in an electric field (E)

F = QE

- The direction of the force is determined by the charge.
- If the charge is **positive**, the force is the **same** direction as the E field.
- If the charge is negative, the force is in the opposite direction to the E field.
- The force on the charge will cause the charged particle to accelerate if it is in the same direction as the E field, or decelerate if in the opposite.

## 18.2 Uniform electric fields

Candidates should be able to:

recall and use  $E = \Delta V / \Delta d$  to calculate the field strength of the uniform field between charged parallel plates

- 2 describe the effect of a uniform electric field on the motion of charged particles
  - The electric field strength (E) of a uniform field between two charged parallel plates is defined as:

$$E = \frac{\Delta V}{\Delta d}$$

Where  $\Delta V$  is the potential difference between the plates and  $\Delta d$  is the separation between plates (m).

- E is now also defined by the units Vm<sup>-1</sup>
- The equation above can only be used for two charged parallel plates.
- A charged particle will move through an electric field due to a force on it that is caused by said electric field.



- The trajectory, as shown in the diagram above is **parabolic**.
- The direction of parabola depends on the charged of the particle.
- In the diagram above, the charge is **negative** hence it is deflected to the **positive** side of the plate.
- If the charge was **positive**, it would have deflected to the **negative** side.
- The amount of deflection depends on three things:

-Mass: the greater the mass, the smaller the deflection and vice versa

-**Charge**: the greater the magnitude of the charge of the particle, the greater the deflection and vice versa

-**Speed**: the greater the speed of the particle, the smaller the deflection and vice versa.

# 18.3 Electric force between point charges (this should be taught after 18.4 or before 18.1)

Candidates should be able to:

- understand that, for a point outside a spherical conductor, the charge on the sphere may be considered to be a point charge at its centre
- 2 recall and use Coulomb's law  $F = Q_1 Q_2 / (4\pi \varepsilon_0 r^2)$  for the force between two point charges in free space
  - Coulomb's Law states that the electrostatic force (F) between two point charges is proportional to the product of the charges and inversely proportional to the square of their separation.
  - The coulomb equation is defined as

$$F = \frac{Q_1 Q_2}{4\pi\varepsilon_0 r^2}$$

Here  $Q_1$  and  $Q_2$  are the point charges (C),  $\varepsilon_0$  is the permittivity of free space (8.85×10<sup>-12</sup> Fm<sup>-1</sup>), r is the distance from the centre of the point charge (m).

- If there is a **positive** and **negative** charge, then the electrostatic force is **negative** (attractive).
- If the charges are the same, they are positive (repulsive)
- The equation above is analogous to Newton's Law of Gravitation Force (F =  $Gm_1m/r^2$ ).

#### 18.4 Electric field of a point charge (this should be right after 18.2!)

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Candidates should be able to:

1 recall and use E = Q / (4\pi\varepsilon_0 r^2) for the electric field strength due to a point charge in free space
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• The electric field at a distance (r) due to a point charge (Q) in free space is defined by

$$E = \frac{Q}{4\pi\varepsilon_0 r^2}$$

• This equation is only used for electric field around a point charge.

• This equation is analogous to the gravitational field strength ( $g = Gm_1/r^2$ ) around a point mass.

#### 18.5 Electric potential

Candidates should be able to:

- 1 define electric potential at a point as the work done per unit positive charge in bringing a small test charge from infinity to the point
- 2 recall and use the fact that the electric field at a point is equal to the negative of potential gradient at that point
- 3 use  $V = Q/(4\pi\varepsilon_0 r)$  for the electric potential in the field due to a point charge
- 4 understand how the concept of electric potential leads to the electric potential energy of two point charges and use  $E_p = Qq / (4\pi\epsilon_0 r)$ 
  - Electric potential is defined as the work done per unit positive charge in bringing a small test charge from infinity to a defined point.
  - Electric potential is a scalar quantity.
  - Although electric potential (V) is a scalar quantity it can have a **negative** or **positive** sign.
  - The electric potential in the field due to a point charge is defined as:

$$V = \frac{Q}{4\pi\varepsilon_0 r}$$

- Here Q is the point charge producing the charge (C)
- This equation is analogous to gravitational potential equation ( $\phi = -Gm_1/r$ ).
- The electric potential energy (EPE or  $E_p$ ) is the work done in bringing a charge from infinity to that point

$$EPE = \frac{Q_1 Q_2}{4\pi\varepsilon_0 r}$$

• The equation above is the work done to move point charge  $Q_2$  from infinity towards point charge  $Q_1$ .

If you want to calculate change in potential energy ( $\Delta$ EPE) from a distance  $r_1$  to a distance  $r_2$  use the following equation

$$\Delta E_p = \frac{Q_1 Q_2}{4\pi\varepsilon_0} \left(\frac{1}{r_1} - \frac{1}{r_2}\right)$$